

$$\begin{aligned} \text{Si: } X(z) &= \sum_{k=-\infty}^{+\infty} x_k z^{-k} \\ &= \sum_{k=-\infty}^{-1} x_k z^{-k} + \sum_{k=0}^{\infty} x_k z^{-k} \\ &= \sum_{k=1}^{\infty} x_{-k} z^k + \sum_{k=0}^{\infty} x_k z^{-k} \end{aligned}$$

Cauchy $\rightarrow \lim_{k \rightarrow \infty} |x_{-k} z^k|^{1/k} < 1 \Rightarrow z < z_0$

et $\rightarrow \lim_{k \rightarrow \infty} |x_k z^{-k}|^{1/k} < 1 \Rightarrow z > z_1$

Domaine de convergence \mathcal{D} .

$$z_0 < z < z_1$$

Remarque

$$z = e^{2\pi j f} \quad |z| = 1 \subset \mathcal{D}.$$